

[Greuling-Goertzel FWHM]  
 (Chapter 1.10.4 in *Elements*)

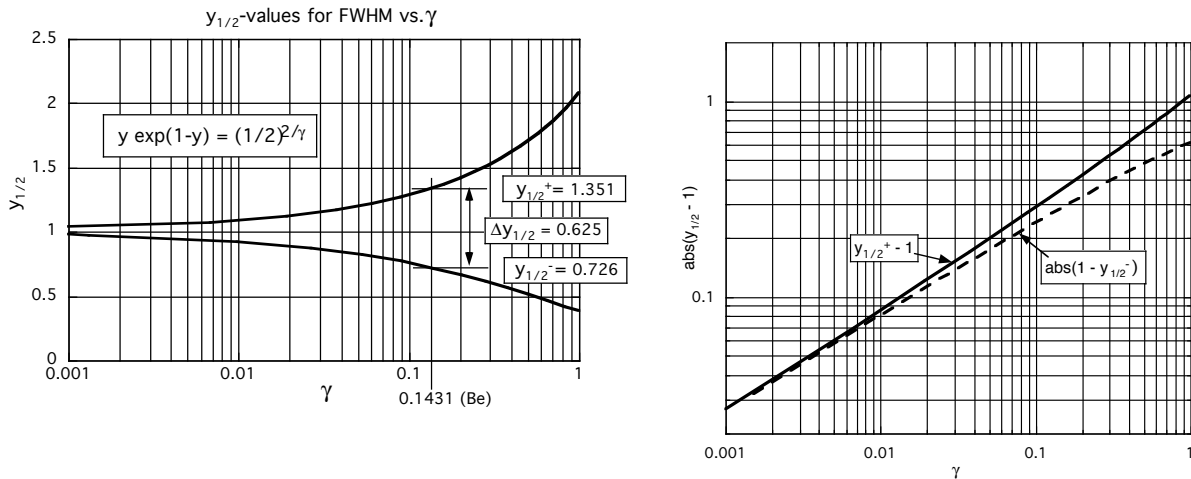
The full width at half maximum, FWHM, of the slowing-down time distribution is given by the difference  $\Delta y_{1/2}$  between the two solutions  $y_{1/2}^+$  and  $y_{1/2}^-$  of the equation

$$y \exp(1 - y) = (1/2)^{1/\gamma} \quad ; \quad (1)$$

that is,

$$FWHM = \Delta y_{1/2} = y_{1/2}^+ - y_{1/2}^- \quad (2)$$

Solving this awkward equation for  $y$  given  $\gamma$  involves *Lambert's W function*,  $z = W(z)\exp(W(z))$  (Corless et al. 1996), little known in practice until recently, and its inverse, which are accessible in modern automated mathematics libraries such as *Mathematica*. The following figure suggests a graphical solution (it is easy to solve the equation for  $\gamma$  for given  $y$ ), illustrating the result  $\Delta y_{1/2}$  for beryllium (consult the table in [Slowing-down Parameters]), which is universally used as a reflector in pulsed-neutron sources.



The values of  $y_{1/2}$  at the half-maximum points of the emission time distribution as functions of  $\gamma$ . Left,  $y_{1/2}^+$  and  $y_{1/2}^-$  vs.  $\gamma$ . Right,  $y_{1/2}^+ - 1$  and  $1 - y_{1/2}^-$  vs.  $\gamma$ , shown to enable accurate reading.

The right panel enables accurate reading of  $\Delta y_{1/2}$  as

$$FWHM = \Delta y_{1/2} = |y_{1/2}^+ - 1| + |1 - y_{1/2}^-| \quad (3)$$